

III B.Tech II Semester(R05) Supplementary Examinations, May 2010
ANALYSIS OF LINEAR SYSTEMS
(Electrical & Electronic Engineering)

Time: 3 hours

Max Marks: 80

Answer any FIVE Questions
All Questions carry equal marks

1. (a) Verify the systems, whose input $x(t)$ and $y(t)$ are related by $y(t) = x^2(t)$ is linear or not?
 (b) Consider the following system described by the input-output relations, are static or dynamic?
 i. $y(t) = \frac{1}{m} \int_{-\infty}^{\infty} x(t) dt$
 ii. $y(t) = e^{xt}$
 (c) Determine whether the following systems are causal or not?
 i. $y(t) = x(-t)$
 ii. $y(t) = x(t) \sin(t+1)$ [4+3+3+3+3]
2. (a) The transfer function of a system is $G(s) = \frac{2}{(s+1)(s+2)}$ obtain the state variable representation of the systems. [8+8]
 (b) Determine the state transition matrix for the system represented by the characteristic matrix

$$A = \begin{bmatrix} 3 & 0 & 0 \\ 0 & -2 & 1 \\ 1 & 4 & 1 \end{bmatrix}$$
3. (a) A pulse voltage of 3V between 1 to 2 sec. is applied to a series R-L circuit with $R=3 \Omega$, $L=1H$, Find the current $i(t)$.
 (b) Find the current $i(t)$ in a series R-L-C circuit with $R=3 \Omega$, $L=1H$, $C=\frac{1}{2}F$ when it is driven by an impulse voltage of $\delta(t-2)$. [6+10]
4. (a) Find the convolution of two identical rectangular pulses. Each rectangular pulse has unit magnitude and duration equal to T seconds starting from $t=0$ seconds.
 (b) Find the convolution of $h(t)=t$ and $f(t)=e^{-at}$ for $t > 0$ [8+8]
5. (a) Derive the expression for RMS value of a complex (of voltage) wave which is expressed in terms of fourier series.
 (b) A complex voltage $e(t) = 100 \sin w t + 30 \sin 3wt + 20 \sin 5 wt$ where $w = 100t$. If this voltage is applied to a load of 10 ohms in series with 0.01H, find the current, average power and power factor of the circuit. [6+10]
6. (a) Find the Fourier transform of
 $F(t) = u(t+T) - u(t-T)$
 (b) Find the Fourier transform of
 $F(t) = 1 - |t/a|$ for $-a < t < a$
 $= 0$ for $|t| > a$ [8+8]
7. (a) Check whether the following polynomial is Hurwitz or not?
 $P(s) = 2s^4 + 5s^3 + 6s^2 + 2s + 1$
 (b) "All driving point immittances of passive networks are positive real functions". Substantiate the statement.
 (c) State the analytical tests to be considered for a polynomial to check whether it is a positive real function or not? [7+5+4]
8. (a) Explain how the removal of pole at infinity of an impedance $Z(s)$ can realize an element in the network.
 (b) Realize the network with the following driving point impedance function using first Foster form.
 $Z(s) = (s+2) / s(2s+5)$ [8+8]
